

$$\tilde{H} \equiv H \left(1 - \frac{\beta(\phi)}{M} \frac{\dot{\phi}}{H} \right)$$